Semina for Osaka U.

Lattice gauge theory with quantum computers



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Outline

- 1. The sign problem in Quantum field theory 4P
- 2. Quantum computer 5P
- 3. Schwinger model with lattice-Hamiltonian formalism ^{10P}
- 4. Adiabatic preparation of vacuum
- 5. Results

6P

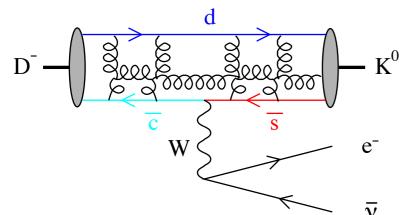
Outline

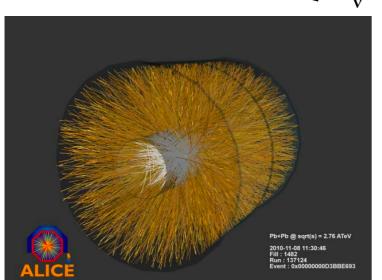
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 - formalism
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Motivation, Big goal Non-perturbative calculation of QCD is important

QCD in 3 + 1 dimension $S = \int d^4x \left[-\frac{1}{4} \text{tr } F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\partial - gA - m) \psi \right]$ $Z = \int \mathscr{D}A \mathscr{D}\bar{\psi} \mathscr{D}\psi e^{iS} \qquad F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu} - ig[A_{\mu}, A_{\nu}]$





- This describes...
 - inside of hadrons (bound state of quarks), mass of them
 - scattering of gluons, quarks
 - Equation of state of neutron stars, Heavy ion collisions, etc
- Non-perturbative effects are essential. How can we deal with?
 - Confinement (閉じ込め)
 - Chiral symmetry breaking (カイラル対称性の自発的破れ)

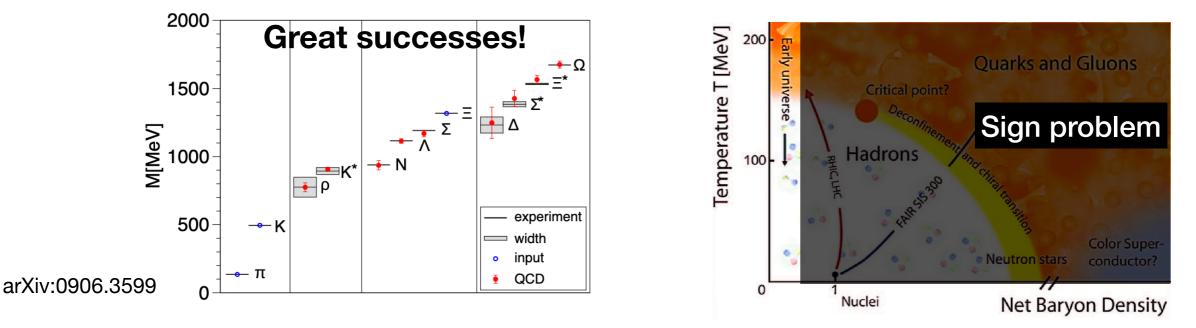
Motivation, Big goal Akio Tomiya LQCD = Non-perturbative calculation of QCD QCD in 3 + 1 dimension $S = \left[d^4 x \left[-\frac{1}{4} \operatorname{tr} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (\mathrm{i}\partial - gA - m) \psi \right] \right]$ $Z = \left[\mathscr{D}A \mathscr{D}\bar{\psi} \mathscr{D}\psi e^{iS} \qquad F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu} - ig[A_{\mu}, A_{\nu}] \right]$ QCD in Euclidean 4 dimension 🕶 $S = \left[d^4 x \left[+ \frac{1}{\Delta} \operatorname{tr} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (\partial - gA - m) \psi \right] \right]$ $Z = \int \mathscr{D}A \mathscr{D}\bar{\psi} \mathscr{D}\psi e^{-S} \quad \leftarrow \text{This can be regarded} \\ \text{as a statistical system}$

- Standard approach: Lattice QCD with Imaginary time and Monte-Carlo
 - LQCD = QCD + cutoff + irrelevant ops. = "Statistical mechanics"
 - Mathematically well-defined quantum field theory
 - Quantitative results are available = Systematic errors are controlled

Motivation, Big goal Sign problem prevents using Monte-Carlo

• Monte-Carlo is very powerful method to evaluate expectation values for "statistical system", like lattice QCD in imaginary time

$$\langle O[U] \rangle = \frac{1}{N_{\text{conf}}} \sum_{c}^{N_{\text{conf}}} O[U_c] + \mathcal{O}(\frac{1}{\sqrt{N_{\text{conf}}}}) \qquad U_c \leftarrow P(U) = \frac{1}{Z} e^{-S[U]} \in \mathbb{R}_+$$



- However, if we have, real time, finite theta, finite baryon density case, we cannot we use Monte-Carlo technique because e^{-S} becomes complex. This is no more probability.
- Hamiltonian formalism does not have such problem! But it requires huge memory to store quantum states, which cannot realized even on supercomputer.
- Quantum states should not be realized on classical computer but on quantum computer (Feynman 1982)

- QCD describes perturbative and non-perturbative phenomena
- Lattice QCD with imaginary time is non-perturbative and quantitive method, which is evaluated by Monte-Carlo
- Sign problem, which is occurred in real time/finite theta/finite baryon density cace, prevents us to use the Monte-Carlo
- Hamiltonian formalism is one solution but we cannot construct the Hilbert space because of the dimensionality
- Quantum simulation/computer is natural realization the Hamiltonian formalism

Question?

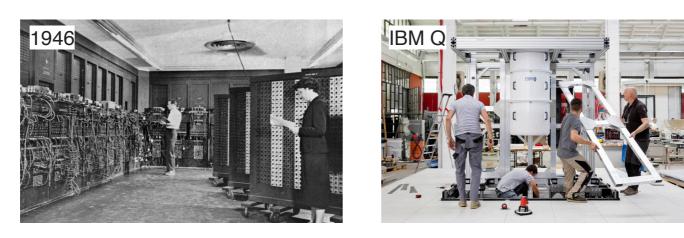
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✓. The sign problem in Quantum field theory 4P ✓. Quantum computer 5P One 3. Schwinger model with lattice-Hamiltonian formalism 10P ✓. Adiabatic preparation of vacuum 3P One 5. Results 6P

Quantum computer? Towards beyond classical computers

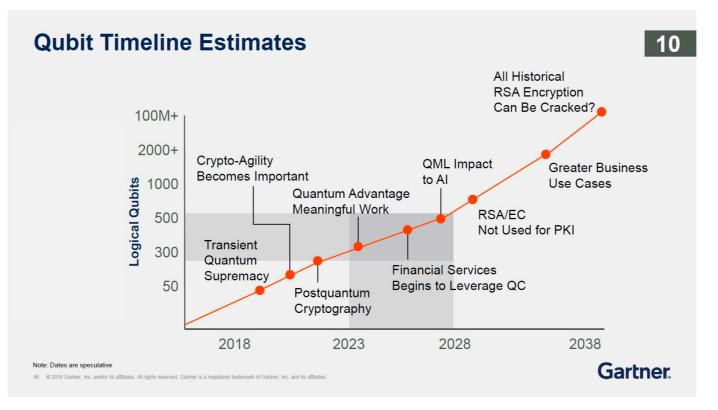
0,1

Data →Machine→Data



 $|0\rangle, |1\rangle$

State →Machine→State



Lattice gauge theory with quantum computer could be a future "common tool"

https://uk.pcmag.com/forward-thinking/117979/gartners-top-10-strategic-technology-trends

Schwinger model with QC

Quantum computer?

For physicists : Circuit ~ time evolution of quantum spins

Toy example of usage of quantum computer

Transverse Ising model on 3 sites (Open boundary)

$$H = -\sum_{\langle j,k \rangle} Z_j Z_k - h \sum_j X_j = -Z_0 Z_1 - Z_1 Z_2 - h X_0 - h X_1 - h X_2$$

$$K_j = -Z_0 Z_1 - Z_1 Z_2 - h X_0 - h X_1 - h X_2$$

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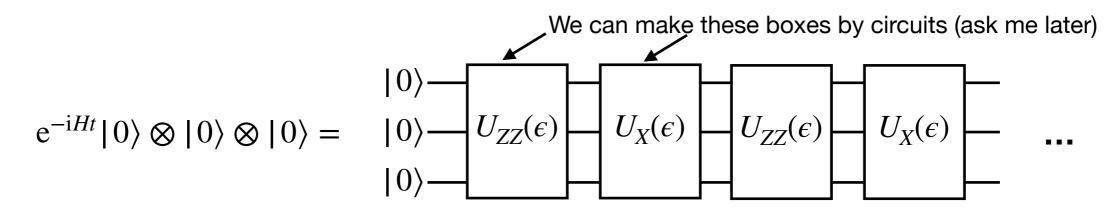
Time evolution for infinitesimal (real) time ε :

$$e^{-iH\epsilon} = e^{-i(-Z_0Z_1 - Z_1Z_2 - hX_0 - hX_1 - hX_2)\epsilon}$$

$$Z_j$$
: Pauli matrix of z on site j
h: size of external field

X: Pauli matrix of x on site i

 $\approx \underbrace{e^{-i(-Z_0Z_1-Z_1Z_2)\epsilon}}_{\equiv U_{ZZ}(\epsilon)} \underbrace{e^{-i(-hX_0-hX_1-hX_2)\epsilon}}_{\equiv U_X(\epsilon)} + O(\epsilon^2) \quad \text{(Suzuki-Trotter expansion)}$



In this way, we can (re)produce, Hamiltonian time evolution using a quantum circuit. Here we can evaluate the systematic error from the expansion and reduce it by using higher order decomposition (leapfrog etc) Quantum computer actually can realize any unitary transformation (skipping proof)

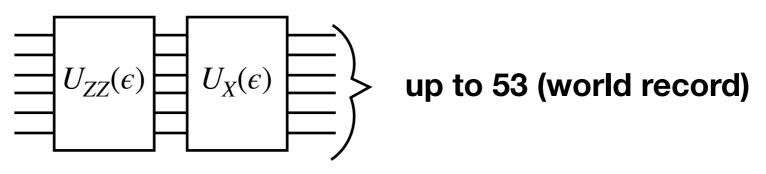
Quantum computer?

Quantum computer is under developing

Quantum computer is theoretically universal, namely it can mimic <u>any</u> unitary transformation, but practically ...

Quantum states are fragile.

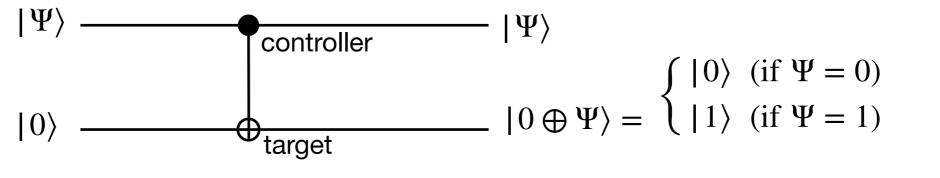
= The number of qubits are not many.



Gate operations are inaccurate.

= We cannot make quantum circuit deeper.

e.g.) <u>Control-not (CNOT) gate</u> If ● side is 0, gate does nothing on the target ⊕ If ● side is 1, gate flips the target ⊕ side.



 $|_{actual} \langle 0 \oplus \Psi | 0 \oplus \Psi \rangle_{ideal} | \approx 0.9$ (machine dependent, 1903.10963)

Operations are sometimes wrongly performed.

In order to study machine independent parts, we use a simulator instead of real one.

From Browser to real machine

Quantum computer? IBM Q is available and free

From Jupyter/python

het camp2019 Last Checkpoint: 2019/10/12 (unsaved changes Q IBM Q Experience - Composer | X + ☆ 🚇 🗉 😋 C auantum-computing.jbm.com/composer/bc18a681e3884ad153e42bc82f400234 Edit View Insert Cell Kernel Widaets Heln Python 3 (1 m + 3≪ 2²1 🖪 ↑ 🖌 N Bun 🔳 C 🕨 Code IBM O Experience S My first circuit Clear New Save Delete Help tutorial My first circuit In [1]: from sympy import import math import matplotlib.pyplot as plt í Visualizations Circuit compose %matplotlib inline from qiskit import QuantumRegister, ClassicalRegister, QuantumCircuit Gate Statevector \sim from qiskit import IBMQ, Aer, execute Statevecto 1 q = QuantumRegister(1) In [2]: qc = QuantumCircuit(q) qc.x(q[0]) 5.0 4 qc.draw(output='mpl') 4.0 3.0 Out[2] nG0 + Add 2.0 q0:|0) X 1.0 q = QuantumRegister(1) In [3]: qc = QuantumCircuit(q)The height of the bar is the qc.z(q[0]) ac draw(output='mpl') complex modulus The color of the bar is based

Several frameworks are available; Qiskit : *de facto* standard (IBM) Qulacs : Fastest simulator (QunaSys, Japan) Blueqat : I think this is easiest (MDR, Japan) etc...

Short summary Quantum computer?

- Quantum computer is developing technology. Current one is noisy so far
- Once hamiltonian is constructed, we can perform time evolution using quantum circuit in principle
- Comment1: We use simulator but our technology can be used in future machines with error-correction. Time resolves this problem.
- Comment2: Simulation of quantum computer by classical machine is generally exponentially hard. To calculate large problem, we need real device.

Question?

Outline

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Schwinger model =2D QED: Solvable at m=0, similar to QCD in 4D.

Schwinger model = QED in 1+1 dimension

$$S = \int d^2x \left[-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\partial - gA - m) \psi + \frac{g\theta}{4\pi} \epsilon_{\mu\nu} F^{\mu\nu} \right]$$

Similarities to QCD in 3+1

- Confinement
- Chiral symmetry breaking (different mechanism)
- Theta term is essential for CP violation and causes the sign problem but in this talk we omit this one (please refer our paper for $\theta \neq 0$)
- Vacuum decay by external electric field (Schwinger effect)

Schwinger model = 2D QED: Solvable at m=0, similar to QCD in 4D.

Schwinger model = QED in 1+1 dimension

$$S = \int d^2x \left[-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\partial - gA - m) \psi \right]$$

 In 1+1 D, Coulomb potential is linear in x, Electric field of a point particle is constant in x

$$E(x)$$
Confinement
$$X$$

2) Chiral condensate is non-zero even for massless fermion, analytical result for massless case

$$\langle \overline{\psi}\psi \rangle = -\frac{e^{\gamma}g}{\pi^{3/2}} = -g0.16\cdots$$
 Chiral symmetry breaking

[Y. Hosotani,...]

Hamiltonian of Schwinger model =2D QED: Solvable at m=0, similar to QCD in 4D.

Schwinger model = QED in 1+1 dimension

$$S = \int d^2x \left[-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\partial - gA - m) \psi \right]$$

- Strategy
 - 1. Derive Hamiltonian with gauge fixing
 - 2. Rewrite gauge field to fermions using Gauss' law
 - 3. Use Jordan-Wigner transformation \rightarrow Spin system

Hamiltonian of Schwinger model What I want explain in this section

Schwinger model = QED in 1+1 dimension

$$S = \int d^2x \left[-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\partial - gA - m) \psi \right]$$

• Strategy(1gauge fix, 2Gauss' law, 3Jordan-Wigner trf)

Schwinger model on the lattice (staggered fermion, OBC, Spin rep.)

$$H = \frac{1}{4a} \sum_{n} \left[X_n X_{n+1} + Y_n Y_{n+1} \right] + \frac{m}{2} \sum_{n} (-1)^n Z_n + \frac{g^2 a}{2} \sum_{n} \left[\sum_{j=1}^n \left(\frac{Z_j + (-1)^j}{2} \right) + \epsilon_0 \right]^2$$

$$e^{-iH\epsilon} \approx e^{-iH_Z\epsilon}e^{-iH_{XX}\epsilon}e^{-iH_{YY}\epsilon}e^{-iH_{ZZ}\epsilon}e^{-iH_{$$

$$U_{Z_j Z_k}(\alpha) = e^{\alpha i Z_j Z_k} = \begin{cases} j & f \\ k & f \\ k & f \\ R_z(2\alpha) &$$

Hamiltonian of Schwinger model =2D QED: Solvable at m=0, similar to QCD in 4D.

(detail)

Schwinger model = QED in 1+1 dimension

$$S = \int d^2x \left[-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\psi} (i\partial - gA - m) \psi \right]$$

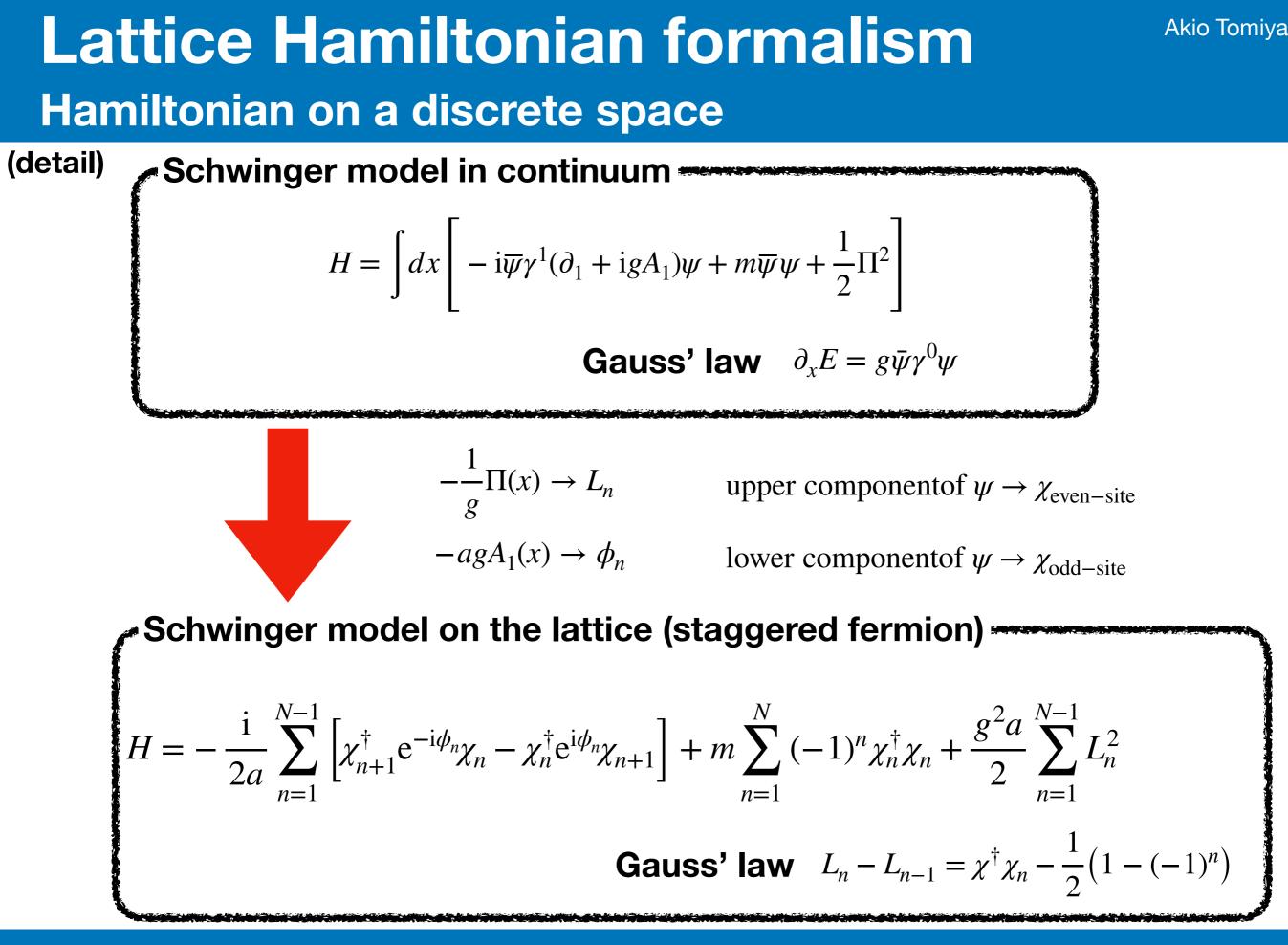
$$\Pi(x) = \frac{\partial \mathscr{L}}{\partial \dot{A}^{1}(x)} = \dot{A}(x) = E(x)$$

$$A_{0} = 0$$

$$H = \int dx \left[-i\overline{\psi}\gamma^{1}(\partial_{1} + igA_{1})\psi + m\overline{\psi}\psi + \frac{1}{2}\Pi^{2} \right]$$

$$\partial_{x}E = g\overline{\psi}\gamma^{0}\psi \qquad \text{(Gauss' law constraint)}$$

This constrains time evolution to be gauge invariant



Lattice Schwinger model

We requires anticommutations to fermions

(detail)

Schwinger model on the lattice (staggered fermion, OBC)

$$H = -\frac{i}{2a} \sum_{n} \left[\chi_{n+1}^{\dagger} \chi_n - \chi_n^{\dagger} \chi_{n+1} \right] + m \sum_{n} (-1)^n \chi_n^{\dagger} \chi_n + \frac{g^2 a}{2} \sum_{n} \left[\sum_{j}^n \left(\chi_j^{\dagger} \chi_j - \frac{1 - (-1)^j}{2} \right) + \epsilon_0 \right]^2$$

System is quantized by assuming the canonical anti-commutation relation

$$\{\chi_j^{\dagger}, \chi_k\} = \mathrm{i}\delta_{jk}$$
 $j, k = \mathrm{site index}$

On the other hand, Pauli matrices satisfy anti-commutation as well

$$\{\sigma^{\mu},\sigma^{\nu}\}=2\delta_{\mu\nu}\mathbf{1}\qquad \mu,\nu=1,2,3$$

Quantum spin-chain case, each site has Pauli matrix, but they are "commute". We can absorb difference of statistical property using Jordan Wigner transformation

$$\chi_n = \frac{X_n - iY_n}{2} \prod_{j < n} (iZ_j)$$

 X_j : Pauli matrix of x on site j Y_j : Pauli matrix of y on site j Z_j : Pauli matrix of z on site j

This guarantees the statistical property

This reproduce correct Fock space.

We can rewrite the Hamiltonian in terms of spin-chain

Osaka U. seminar

Schwinger model with QC

Akio Tomiya Lattice Schwinger model = spin system Jordan-Wigner transformation: Fermions ~ Spins (detail) Schwinger model on the lattice (staggered fermion, OBC) - $H = -\frac{i}{2a} \sum_{n} \left[\chi_{n+1}^{\dagger} \chi_{n} - \chi_{n}^{\dagger} \chi_{n+1} \right] + m \sum_{n} (-1)^{n} \chi_{n}^{\dagger} \chi_{n} + \frac{g^{2}a}{2} \sum_{n} \left[\sum_{i}^{n} \left(\chi_{j}^{\dagger} \chi_{j} - \frac{1 - (-1)^{j}}{2} \right) + \epsilon_{0} \right]^{2}$ $\begin{cases} \chi_n = \frac{X_n - iY_n}{2} \prod_{j < n} (iZ_j) \\ \chi_n^{\dagger} = \frac{X_n + iY_n}{2} \prod_{j < n} (-iZ_j) \end{cases}$ Jordan-Wigner transformation X_i : Pauli matrix of x on site j Y_i : Pauli matrix of y on site j Z_i : Pauli matrix of z on site j

Schwinger model on the lattice (staggered fermion, OBC, Spin rep.)

$$H = \frac{1}{4a} \sum_{n} \left[X_n X_{n+1} + Y_n Y_{n+1} \right] + \frac{m}{2} \sum_{n} (-1)^n Z_n + \frac{g^2 a}{2} \sum_{n} \left[\sum_{j=1}^n \left(\frac{Z_j + (-1)^j}{2} \right) + \epsilon_0 \right]^2$$

[Y. Hosotani 9707129]

Schwinger model with QC

Akio Tomiya Lattice Schwinger model = spin system Jordan-Wigner transformation: Fermions ~ Spins (detail) Schwinger model on the lattice (staggered fermion, OBC, Spin rep.) * $H = \frac{1}{4a} \sum_{n} \left[X_n X_{n+1} + Y_n Y_{n+1} \right] + \frac{m}{2} \sum_{n} (-1)^n Z_n + \frac{g^2 a}{2} \sum_{n} \left[\sum_{i=1}^n \left(\frac{Z_j + (-1)^j}{2} \right) + \epsilon_0 \right]^2$ Evolution by each term can be represented by gates (with Suzuki-Trotter expansion): $|0\rangle_{\text{circuit}} = |\uparrow\rangle_{\text{spin}}$ e.g.) $U_{Z_j Z_k}(\alpha) = e^{\alpha i Z_j Z_k} = \int R_z(\theta) = \exp(i\frac{1}{2}\theta\sigma_z)$ $|1\rangle_{\text{circuit}} = |\downarrow\rangle_{\text{spin}}$

Skipping detailed calculation but, this realizes correct unitary evolution

$$U_{Z_0Z_1}(\alpha) |\uparrow\rangle_0 |\uparrow\rangle_1 = e^{\alpha i Z_j Z_k} |\uparrow\rangle_0 |\uparrow\rangle_1 = e^{+\alpha} |\uparrow\rangle_0 |\uparrow\rangle_1$$
$$U_{Z_0Z_1}(\alpha) |\downarrow\rangle_0 |\downarrow\rangle_1 = e^{\alpha i Z_j Z_k} |\downarrow\rangle_0 |\downarrow\rangle_1 = e^{+\alpha} |\downarrow\rangle_0 |\downarrow\rangle_1$$
$$U_{Z_0Z_1}(\alpha) |\downarrow\rangle_0 |\uparrow\rangle_1 = e^{\alpha i Z_j Z_k} |\downarrow\rangle_0 |\uparrow\rangle_1 = e^{-\alpha} |\downarrow\rangle_0 |\uparrow\rangle_1$$
$$U_{Z_0Z_1}(\alpha) |\uparrow\rangle_0 |\downarrow\rangle_1 = e^{\alpha i Z_j Z_k} |\downarrow\rangle_0 |\downarrow\rangle_1 = e^{-\alpha} |\downarrow\rangle_0 |\uparrow\rangle_1$$

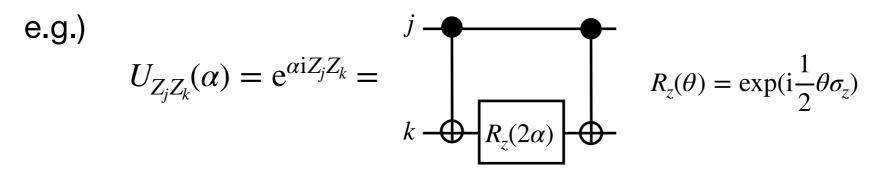
 Lattice Schwinger model = spin system
 Akio Tomiya

 Jordan-Wigner transformation: Fermions ~ Spins
 Akio Tomiya

Schwinger model on the lattice (staggered fermion, OBC, Spin rep.)

$$H = \frac{1}{4a} \sum_{n} \left[X_n X_{n+1} + Y_n Y_{n+1} \right] + \frac{m}{2} \sum_{n} (-1)^n Z_n + \frac{g^2 a}{2} \sum_{n} \left[\sum_{j=1}^n \left(\frac{Z_j + (-1)^j}{2} \right) + \epsilon_0 \right]^2$$

Evolution by each term can be represented by gates (with Suzuki-Trotter expansion):



Then, we can evaluate,

$$e^{-iHt}|0\rangle \otimes |1\rangle \otimes \cdots \otimes |0\rangle \otimes |1\rangle$$

(trivial ground state for m, $g \rightarrow \infty$)

To calculate chiral condensate, we have to prepare the vacuum for full Hamiltonian.

$$|\Omega\rangle_{\text{exact}} \neq |0\rangle \otimes |1\rangle \otimes \cdots \otimes |0\rangle \otimes |1\rangle$$

Next section, we discuss state preparation.

Short summary Lattice Schwinger model = spin system

- Schwinger model, 1+1 dimensional QED, is a toy model for QCD in 3+1 dim.
- Lattice Schwinger model + open boundary = Spin model
- We can realize time evolution of lattice Schwinger model using circuit.
- We want to reproduce analytic value for the chiral condensate at m=0 in the continuum,

$$\langle \overline{\psi}\psi\rangle = -\frac{\mathrm{e}^{r}g}{\pi^{3/2}} = -g0.16\cdots$$

to study usability of quantum computer/circuit

Question?

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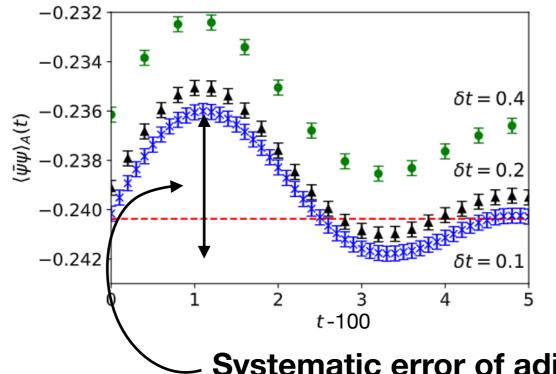
Adiabatic preparation of vacuum To calculate VEV, vacuum is needed

(Following is slightly simplified from our paper, but essentially same)

Adiabatic state preparation

We can control systematic error from adiabatic st. prep.

Adiabatic time T >> 1/gap, it looks converge



- Systematic error	of adiabatic	state preparation
-		

		State prep.	Good	Bad
We u	lse→	Adiabatic	Systematic error is under control. It can be eliminated by extrapolation	Huge cost (Depth is required)
		Variational mmonly used in ant. chemistry)	Economical (Magically good quality)	Depends on ansatz, in principle
Osaka I	U. semina	ır	Schwinger model with QC	

Short summary

Adiabatic state preparation is systematically controlled

- To calculate vacuum expectation values, we need vacuum for full Hamiltonian
- Adiabatic state preparation is costly but sources of systematic errors are clear, safe to use.
- Note: Adiabatic state preparation becomes inefficient if the system approaches to gapless region ($\theta = \pi$). In the paper, we use improved time evolution operator

Question?

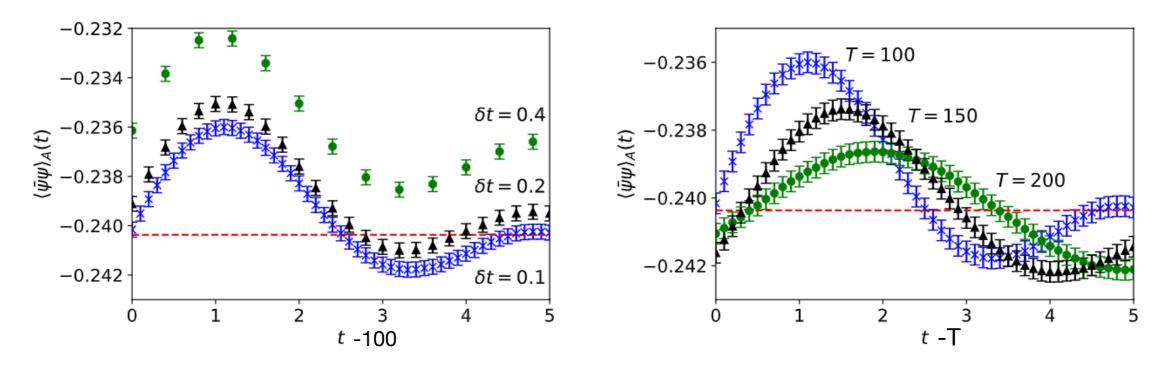
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Results

Chiral condensate with certain limits

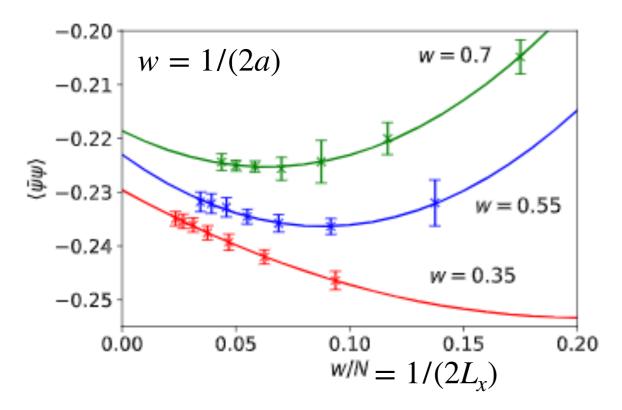
- We calculate chiral condensate for m =0, m>0 in lattice Schwinger model
- We have taken limits,
 - 1. Large volume limit (Nx->0)
 - 2. Continuum limit (a->0)
- Limits for adiabatic state preparation are not taken yet but under control
 - Step size for Trotter decomposition (Left panel)
 - Large adiabatic time lime (Right panel)



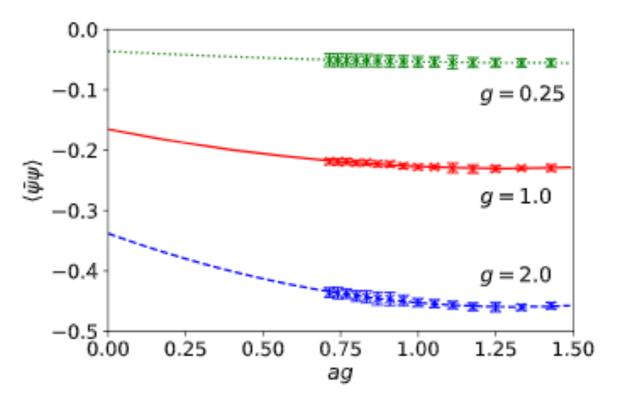
We take step size as 0.1 and adiabatic time as 100

Results: Large vol. & Cont. limit Systematic errors from theory are under control

Large volume limit via state pre.



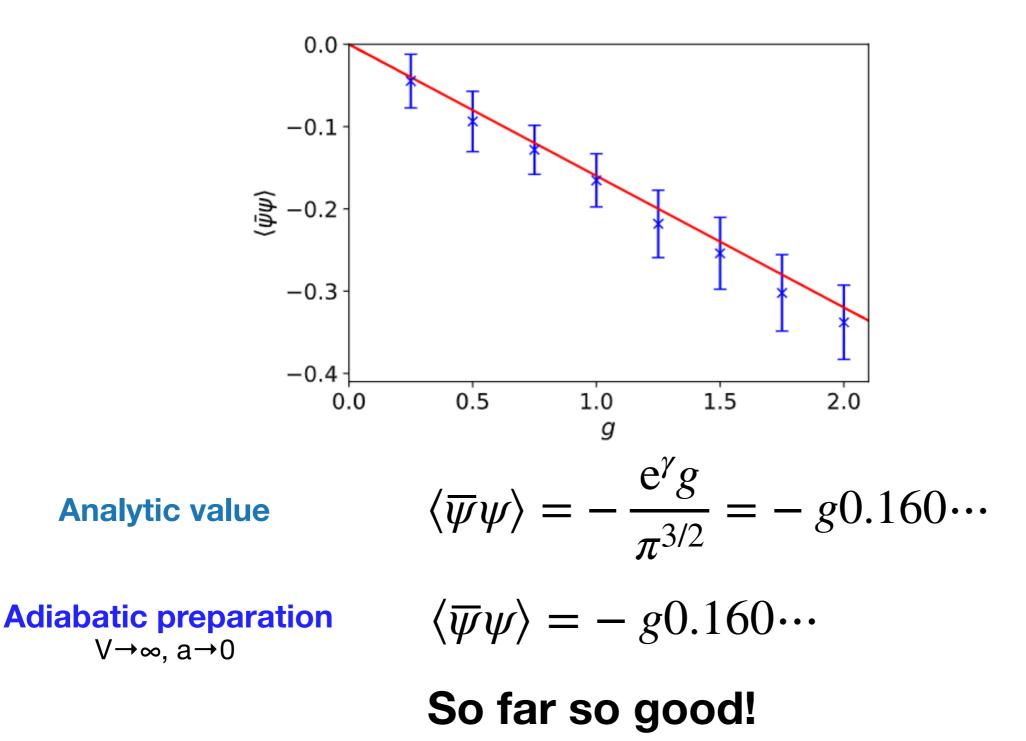
Error bar includes systematic and statistical error. Statistics = 10⁶ shots Continuum limit via state pre.



Error bar are asymptotic error for finite volume limit extrp.

Results: Large vol. & Cont. limit Systematic errors from theory are under control

Results for massless Schwinger model are consistent with analytic value

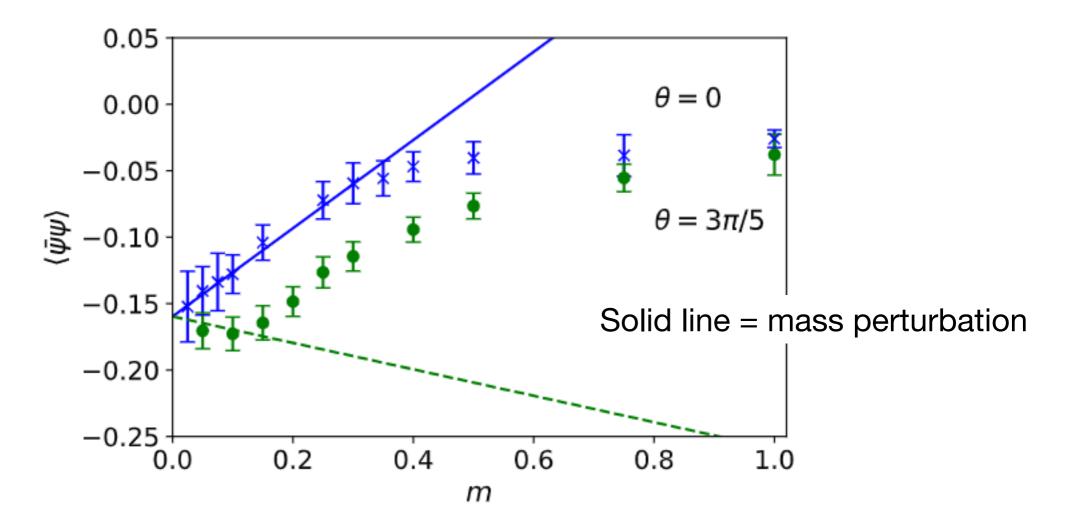


Schwinger model with QC

Results: Large vol. & Cont. limit Systematic errors from theory are under control

Massive case and its time dependence (skipping all details)

For massive case, results via mass perturbation is known. Result depends on θ as well as QCD



Our result for |m| < 1 reproduces mass perturbation as well as theta dependence. Large mass regime, we observe deviation

Schwinger model with QC

Towards on real machine Real machine is noisy

- We need to care the fidelity: "accuracy" of operation of gates on qubits.
- Each time step = 250(# of 1-qubit gates)+270(# of 2-qubit gates)
- The number of time steps = T / δt = 1000
- Each gate operation has error, we need improvement.
 - Hardware side: Error correction, reliable qubits/operations
 - Theory side: improvement of decomposition & annealing process, this is discussed in our paper
- Towards to realize QCD, we need
 - Efficient higher dimensional version of "Jordan-Wigner" transf.
 - Development of treatment for continuous gauge d.o.f.
 - A number of (reliable) qubits
 - Efficient way of state preparation with controlling error

Summary QFT calculation by Quantum computer

- We are investigating chiral condensate in the Schwinger model
- Errors from limits (Large volume, continuum) are under control
- Adiabatic state preparation works well
- We reproduce results both of massless and massive case

• Future work: Other observables, time depending process, etc

Thanks!